

# OptiSystem applications: Photodiode sensitivity modelling



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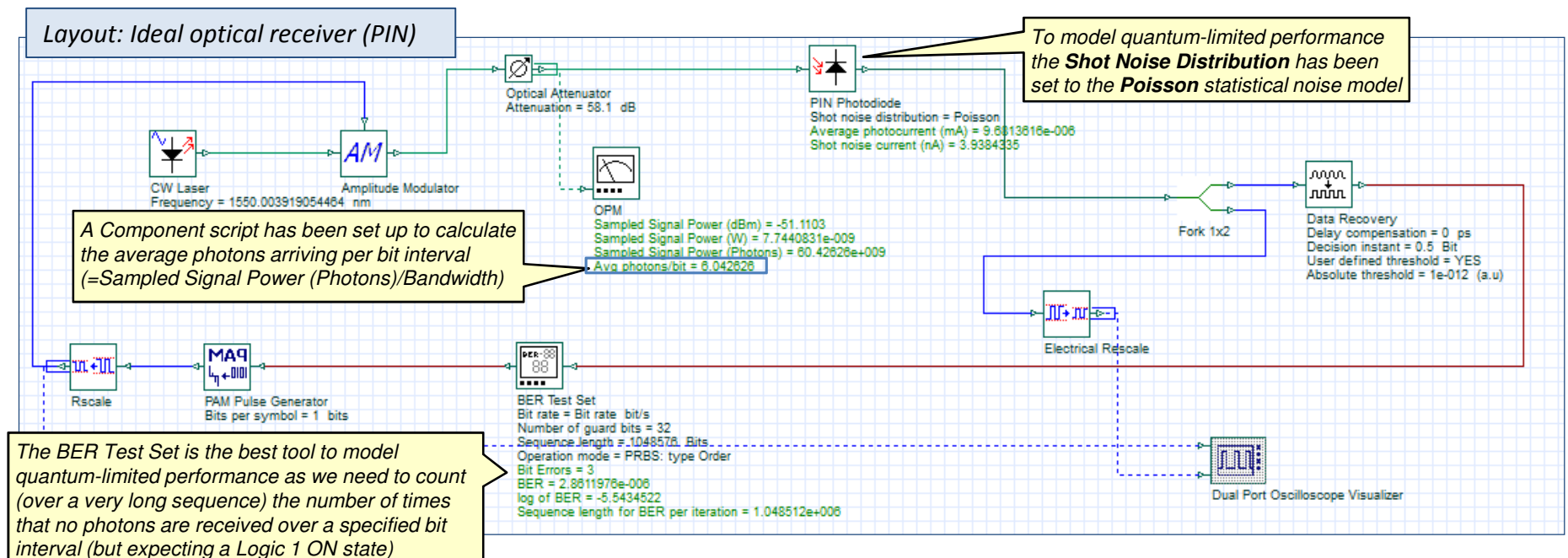


- One of the main working parts of any optical receiver is the photodetector (which converts optical power to an electric current). Either a PIN or APD (avalanche photodiode) photodetector can be used depending on the system performance objectives.
- The **bit error rate (BER)** is the primary metric used to specify the reliability of a communication transmission system and is normally linked to a **Receiver sensitivity** value which defines the minimum average optical power that must reach the photodetector to achieve a desired BER performance. Alternatively the Q of the channel can be calculated from sampled signal statistics and used to estimate the system BER (**OptiSystem** supports both calculation methods).
- The photodetector plays an important role in defining the ultimate sensitivity of a basic communication system as it contributes statistical perturbations in the form of **shot** (quantum-based) and **thermal** noise. It also introduces a dark current (which can be viewed as DC noise) and has a defined **Responsivity** (a measure of how much electrical output is obtained per unit of input power) which depends on the wavelength of the incident light and the sensor's material properties and physical design. In addition to these effects, photodetectors also exhibit a frequency-dependent transfer function due to the presence of a junction capacitance and the need to connect to a load resistor to measure the received signal (for this analysis the transfer function is assumed to be ideal)
- The following four examples demonstrate how to setup and measure (using **OptiSystem**) the receiver sensitivities of PIN and APD intensity-modulated direct-detection (IM-DD) systems, specifically:
  - Quantum-limited ideal PIN photodetector
  - Thermal-noise limited PIN photodetector
  - Thermal and shot-noise APD performance
  - PIN photodetector with optical pre-amplification
- The reference file for this application note is: *PIN and APD Receiver Sensitivity Analysis Version 1\_0 24 Jan 17.osd*.

# Ideal photodetector (PIN)

## Photodetector sensitivity modelling

- The test configuration is as follows : Bit rate: 10 Gb/s; Wavelength = 1550 nm; PIN responsivity: 1 A/W; Dark current = 0 nA; Sequence length = 1048576.
  - As the receiver is ideal its only noise source is the PIN shot (quantum) noise - the thermal noise contribution has been disabled. The receiver makes an error when an expected Logic 1 (ON signal) sees no photons (Poisson statistics). The absolute threshold of the **Data Recovery** component is set to 1E-12 to verify this condition.
  - The minimum number of photons/bit required to achieve a given BER can be calculated as follows:  $BER = 1/2 * \exp(-2*N)$  where N is the average number of photons per bit. For the example below the attenuator was set to 58.1 dB (average photons per bit  $\approx 6$ ). The resulting expected quantum limit performance is  $LOG(BER) = -5.51$ .
  - For the simulation run below, the **BER Test Set** shows that three bit errors were detected ( $LOG(BER) = -5.54$ )
- REF: L. Kazovsky, S. Benedetto, A. Willner, *Optical Fiber Communication Systems*, Artech House (1996), pp. 199-200

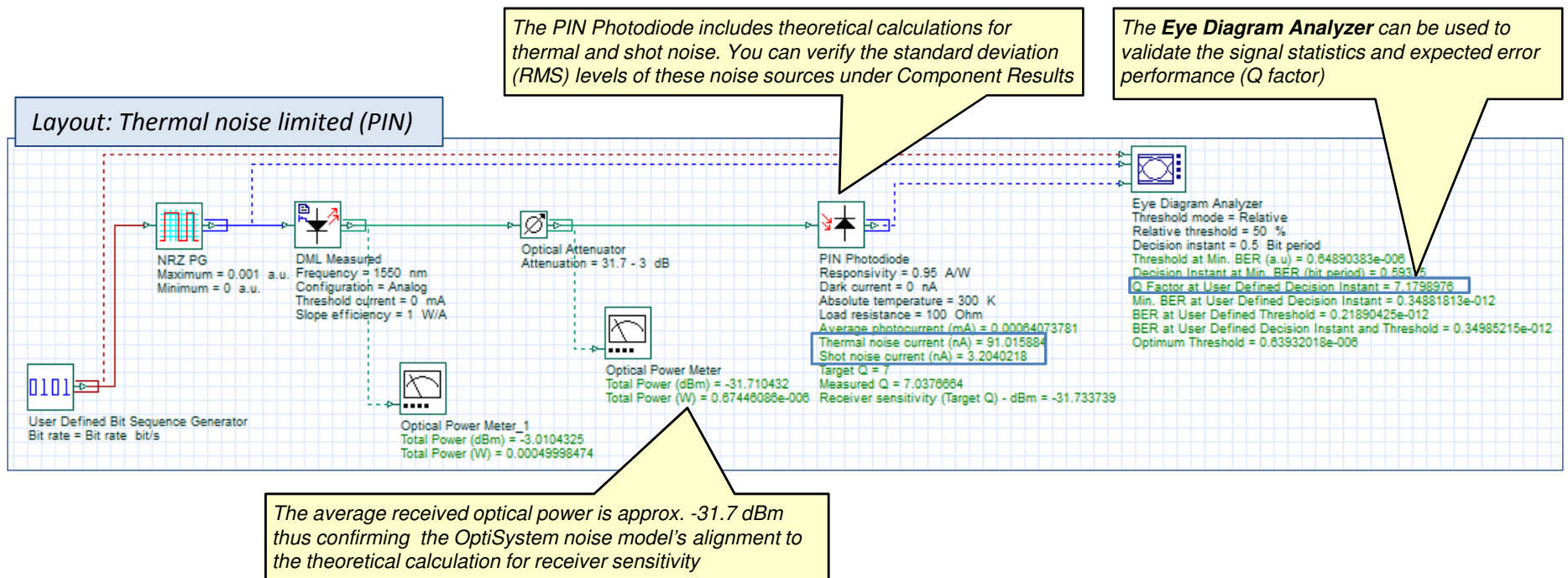


# Thermal noise limited PIN (1)

## Photodetector sensitivity modelling

- In this example the receiver sensitivity of a PIN photodiode (for  $Q=7$ ,  $BER=1E-12$ ) is determined based on the following configuration: Bit rate: 100 Mb/s; Wavelength = 1550 nm; Load resistance: 100 ohm; Temp = 300K; PIN responsivity: 0.95 A/W
- In this case the primary noise source is the PIN thermal noise (Thermal noise current = 91 nA). The required receiver sensitivity is approximately -31.7 dBm.
- NOTE: In the reference the load resistance is set to 200 ohm. As an additional amplifier noise figure of 3 dB is included in the REF (to model an electrical post-amplifier), we have reduced the load resistance to 100 to account for this factor of 2 increase in noise.

REF: Keiser, Gerd; "Optical Fiber Communications", 4th Ed., Tata McGraw Hill, 2008 (pp 261-262)



# Thermal noise limited PIN (2)

- The **Component script** feature can be used to perform custom calculations and results. If needed, parameters or results from any component on the design canvas can be accessed and used as inputs for calculations.
- The VBScript below is associated with the **PIN Component**. The received signal Q is first calculated and then the Receiver sensitivity is calculated based on a target Q (the measured Q can also be used).
- To access the Component script, right-click on the component and select *Component Script* from the pull-down menu

```

Dir ThisComponent
Set ThisComponent = GetThisComponent()

Iaverage = ThisComponent.GetResultValue( "Average photocurrent (mA)" )
ThermalStdDev = ThisComponent.GetResultValue( "Thermal noise current (nA)" )
ShotStdDev = ThisComponent.GetResultValue( "Shot noise current (nA)" )
Resp = ThisComponent.GetParameterValue( "Responsivity" )

Function Log10(X)
Log10 = Log(X) / Log(10)
End Function

' Q = I1/(sigma1+sigma0) = 2*Iavg/(sigma1+sigma0) where "1" represents ON and "0" represents OFF (OOK)
' REF: Keiser, Gerd; "Optical Fiber Communications", 4th Ed., Tata McGraw Hill, 2008 (pp 260-261)
If (ThermalStdDev > 0 OR ShotStdDev > 0) Then
Q = (2*Iaverage*1e-3) / ((sqr((ThermalStdDev*1e-9)^2+(ShotStdDev*1e-9)^2))+(ThermalStdDev*1e-9))
Else
Q = 0
End If

TargetQ = 7 ' (BER = 1e-12)

' Psen = Q*I1/(2R) = Q*(sigma1+sigma0)/(2R)
OpticalSensitivity = TargetQ * ((sqr((ThermalStdDev*1e-9)^2+(ShotStdDev*1e-9)^2))+(ThermalStdDev*1e-9)) / (Resp*2)
If OpticalSensitivity = 0 Then
OpticalSensitivitydBm = -100
Else
OpticalSensitivitydBm = 10*Log10( OpticalSensitivity * 1e3 )
End If

ThisComponent.SetResultValue "Target Q", Cdbl( TargetQ )
ThisComponent.SetResultValue "Measured Q", Cdbl( Q )
ThisComponent.SetResultValue "Receiver sensitivity (Target Q) - dBm", Cdbl( OpticalSensitivitydBm )
    
```

**Access Parameters and Calculation results from PIN Component**

**Calculate Q factor from average received signal photocurrent and RMS levels for Logic 1 (thermal + shot) and Logic 0 (shot noise)**  
 $Q = 2 \cdot I_{avg} / (\sigma_1 + \sigma_0)$

**Calculate Receiver sensitivity:**  
 $RxSen = Q \cdot (\sigma_1 + \sigma_0) / (2 \cdot R)$

**Export results to the Results tab (performed at the end of each simulation run)**

**Note: These custom results need to be manually added to the Component Results!**

| Disp                                | Name  | Value                  |
|-------------------------------------|---|------------------------|
| <input checked="" type="checkbox"/> | Average photocurrent (mA)                           | 0.0006407378148676963  |
| <input type="checkbox"/>            | Thermal noise spectral density (A <sup>2</sup> /Hz) | 0.1656778224e-021      |
| <input checked="" type="checkbox"/> | Thermal noise current (nA)                          | 91.01588388847299      |
| <input type="checkbox"/>            | Shot noise spectral density (A <sup>2</sup> /Hz)    | 0.205315120290952e-024 |
| <input checked="" type="checkbox"/> | Shot noise current (nA)                             | 3.204021849886108      |
| <input type="checkbox"/>            | Noise equivalent power (W/sqrt(Hz))                 | 13.5574345100169e-012  |
| <input type="checkbox"/>            | Modulation bandwidth (GHz)                          | 0                      |
| <input type="checkbox"/>            | Transit time (ps)                                   | 0                      |
| <input checked="" type="checkbox"/> | Target Q  | 7                      |
| <input checked="" type="checkbox"/> | Measured Q  | 7.037666425968212      |
| <input checked="" type="checkbox"/> | Receiver sensitivity (Target Q) - dBm               | -31.73373887597311     |



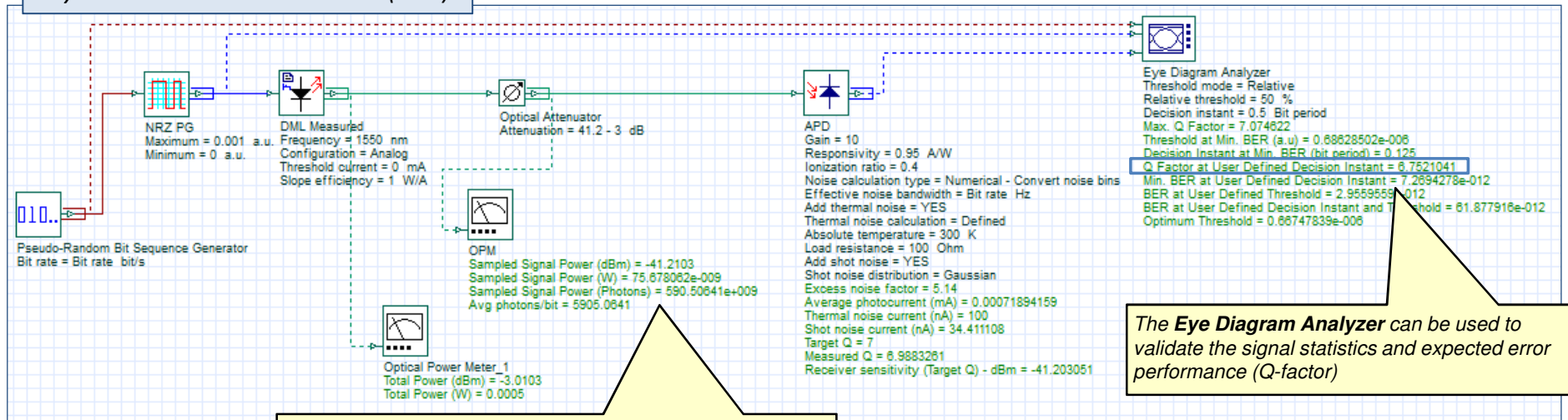
# Thermal/shot noise APD

## Photodetector sensitivity modelling

- In this example the receiver sensitivity of an APD photodiode (for  $Q=7$ ,  $BER=1e-12$ ) is determined based on the following configuration: Bit rate: 100 Mb/s; Wavelength = 1550 nm; Load resistance: 100 ohm; Temp = 300K; PIN responsivity: 0.95 A/W; Gain(M) = 10; F(M) = 5.
- In this case the primary noise source remains the APD thermal noise (Thermal noise current = 100 nA) but the shot noise increases due to the APD gain and excess noise factor (Shot noise current = 21 nA). However, as the signal also undergoes gain the overall performance is improved in comparison to the PIN model (the required receiver sensitivity is approximately -42 dBm).
- NOTE: In the reference the load resistance is set to 200 ohm. As an additional amplifier noise figure of 3 dB is included in the REF (to model an electrical post-amplifier), we have reduced the load resistance to 100 to account for this factor of 2 increase in noise.

REF: Keiser, Gerd; "Optical Fiber Communications", 4th Ed., Tata McGraw Hill, 2008 (pp 261-262)

### Layout: Thermal and Shot Noise (APD)



The average received optical power is approx. -41.2 dBm thus confirming the OptiSystem noise model's alignment to the theoretical calculation for receiver sensitivity

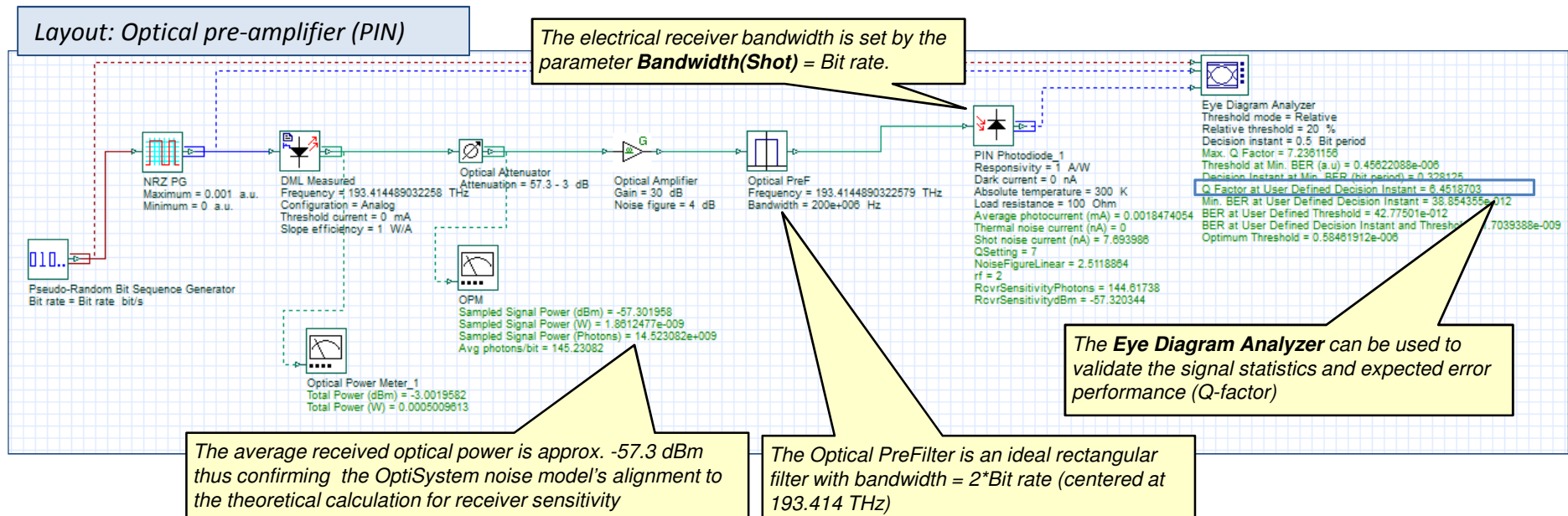
The Eye Diagram Analyzer can be used to validate the signal statistics and expected error performance (Q-factor)

# PIN with Optical Pre-Amp (1)

## Photodetector sensitivity modelling

- In this example the receiver sensitivity of a PIN photodiode with an optical pre-amplifier (for  $Q=7$ ,  $BER=1e-12$ ) is modelled based on the following configuration: Bit rate: 100 Mb/s; Wavelength = 1550 nm (193.4145 THz) ; OA Gain=30 dB; OA\_NF=4 dB; Optical Filter BW =Bitrate\*2; PIN responsivity: 0.95 A/W; Receiver BW = Bit rate
- In this case the primary noise source is assumed to be the signal-ASE beat noise (as we are applying a channel filter after the OA, the ASE-ASE beat noise can be neglected).
- The thermal noise has also been neglected for this analysis but will generally add a degradation especially when the optical power at the receiver is low (less than 1 mW)
- The receiver sensitivity is calculated as follows:  $RcvrSenPwr = NFLinear * h * Freq * RxBW * (Q^2 + Q(rf-0.5))^{0.5}$

REF: *Optical Communication Systems (OPT428)*, slides 280-282, Govind P. Agrawal, Institute of Optics, University of Rochester, Rochester, NY 14627 (<http://www.optics.rochester.edu/users/gpa/opt428c.pdf> - Accessed 9 Jan 2017)



# PIN with Optical Pre-Amp (2)

- The VBScript below is associated with the **PIN Component** (Layout: *Optical pre-amplifier (PIN)*). The optical sensitivity is calculated three ways: Photons per bit, Power (W), Power (dBm)
- The Bandwidth ratio (*rf*) defines the ratio of the optical filter bandwidth to that of the electrical receiver bandwidth (keeping this ratio low helps to improve the receiver sensitivity).

The screenshot shows a VBScript editor window with the following code:

```
Dir ThisComponent
Set ThisComponent = GetThisComponent ()

Iaverage = ThisComponent.GetResultValue( "Average photocurrent (mA)" )
Resp = ThisComponent.GetParameterValue( "Responsivity" )

Q = 7
NFdB = 4
NFLinear = 10^(NFdB/10)
ReceiverBW = 100e6 'Hz
OpticalBW = 200e6 'Hz
rf = OpticalBW/ReceiverBW
h = 6.6260704E-34 'm2*kg / s
Freq = 193.4145e12 'Hz

Function Log10(X)
Log10 = Log(X) / Log(10)
End Function

OpticalSensitivityPhotons = (NFLinear) * ( (Q*Q) + (Q*((rf-0.5)^0.5)) )
OpticalSensitivityPwr = NFLinear*h*Freq*ReceiverBW*((Q*Q) + (Q*((rf-0.5)^0.5)))
OpticalSensitivitydBm = 10*Log10( OpticalSensitivityPwr * 1e3 )

ThisComponent.SetResultValue "QSetting" , Cdbl( Q )
ThisComponent.SetResultValue "NoiseFigureLinear" , Cdbl( NFLinear )
ThisComponent.SetResultValue "rf" , Cdbl( rf )
ThisComponent.SetResultValue "RcvrSensitivityPhotons" , Cdbl( OpticalSensitivityPhotons )
ThisComponent.SetResultValue "RcvrSensitivitydBm" , Cdbl( OpticalSensitivitydBm )
```

Callouts in the image provide the following explanations:

- Access Parameters and Calculation results from PIN component**: Points to the lines `Iaverage = ThisComponent.GetResultValue( "Average photocurrent (mA)" )` and `Resp = ThisComponent.GetParameterValue( "Responsivity" )`.
- Define local variables for calculations. These values can also be accessed from global parameters.**: Points to the variable declarations for `Q`, `NFLinear`, `ReceiverBW`, `OpticalBW`, `rf`, `h`, and `Freq`.
- Calculations for receiver sensitivity (Photons/bit, Power (W), Power (dBm))**: Points to the calculation of `OpticalSensitivityPhotons`, `OpticalSensitivityPwr`, and `OpticalSensitivitydBm`.
- Export results to the Component Results tab (performed at the end of each simulation run)**: Points to the `ThisComponent.SetResultValue` statements at the bottom of the script.